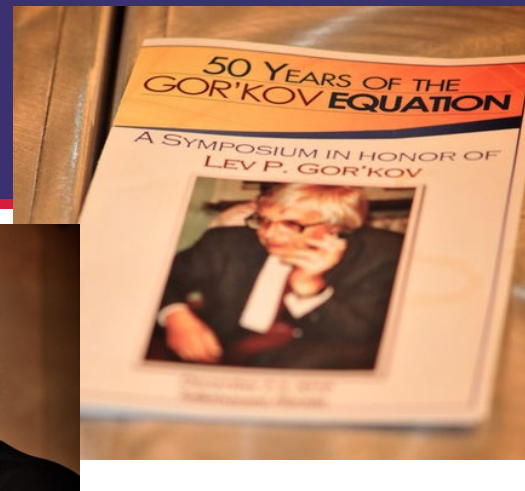




# The 2010 LevFest in Tallahassee



**Celebrating Lev's 80<sup>th</sup> Birthday (when he was 81)  
and Celebrating 50 Years of the Gor'kov Equation**





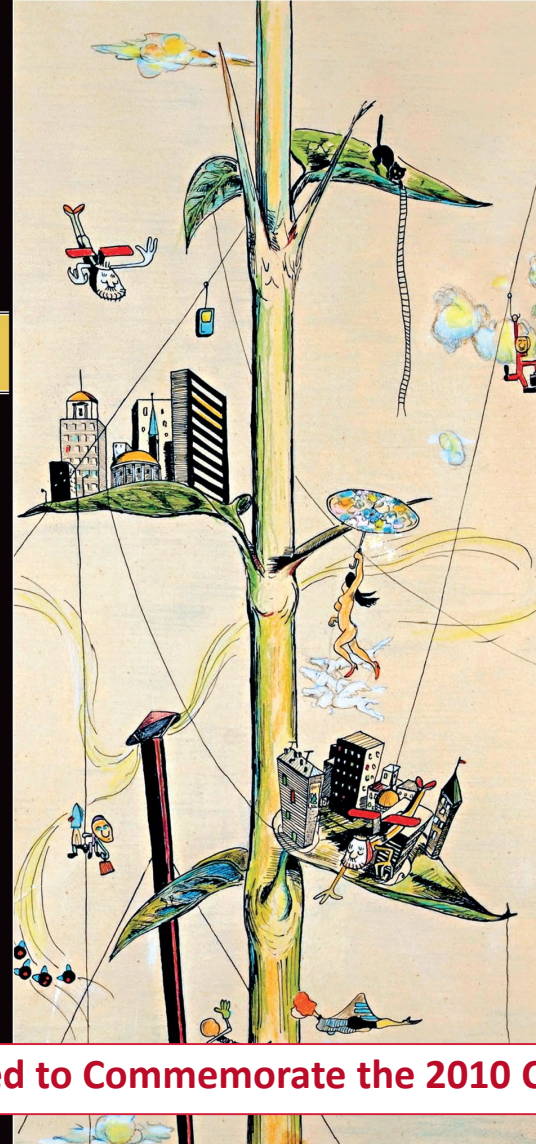
# The 2010 LevFest in Tallahassee



Front cover:  
Stem of Life,  
1964.

LEV GOR'KOV

ILLUSTRATIONS to LIFE



Lev Gor'kov

ILLUSTRATIONS  
to  
LIFE

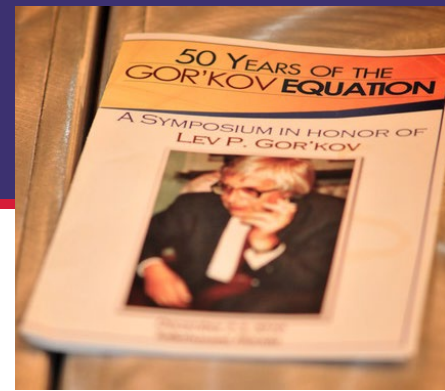


The Untitled Drawing  
on the Back Cover

Compiled to Commemorate the 2010 Celebration



# The 2010 LevFest in Tallahassee



**What was it like to be Lev's "boss"? (His word. Not mine!)**

**1. The university bureaucracy insisted that I evaluate Lev's work:**

**Lev: "Here, boss, this is a list of what I have tried to accomplish this year."**

**Greg: "This exceeds Florida State University's high performance standards."**

**2. Virtually every interaction**

**(a) began with a smile and  
(b) ended with laughter.**



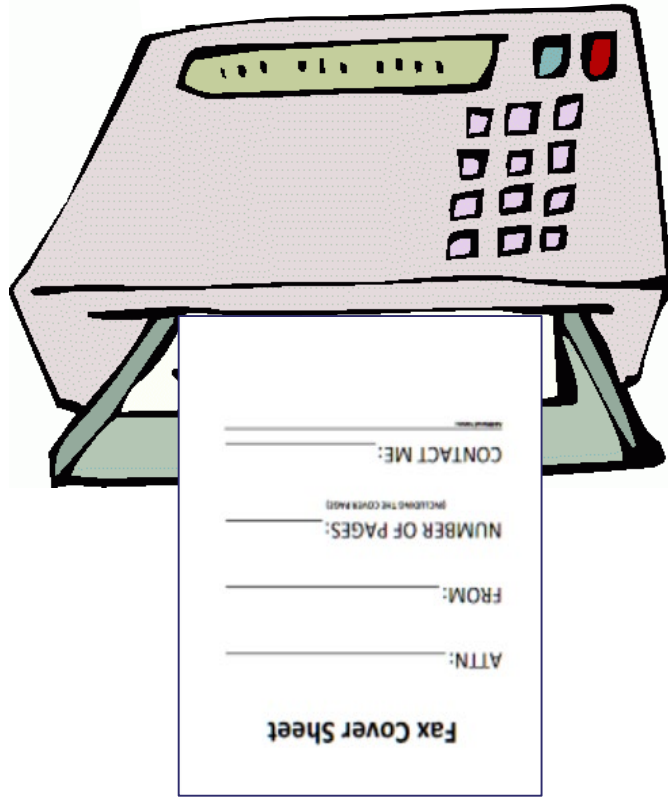
**3. When Lev laughed, I almost always understood what he was laughing about.**

**When Lev smiled broadly, I thought I understood only 50% of the time...**

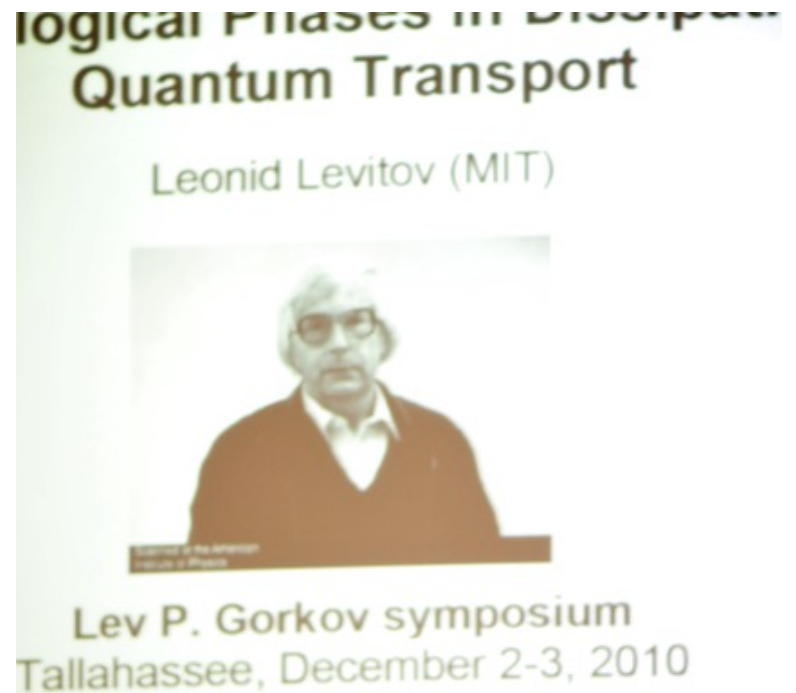
**...but when Lev was only smiling a little...**



# The First Time I Encountered Lev Gor'kov (1990)



**Greg's Story: Fuzzy Dot-Matrix Paper Emerging from Fax Machine**

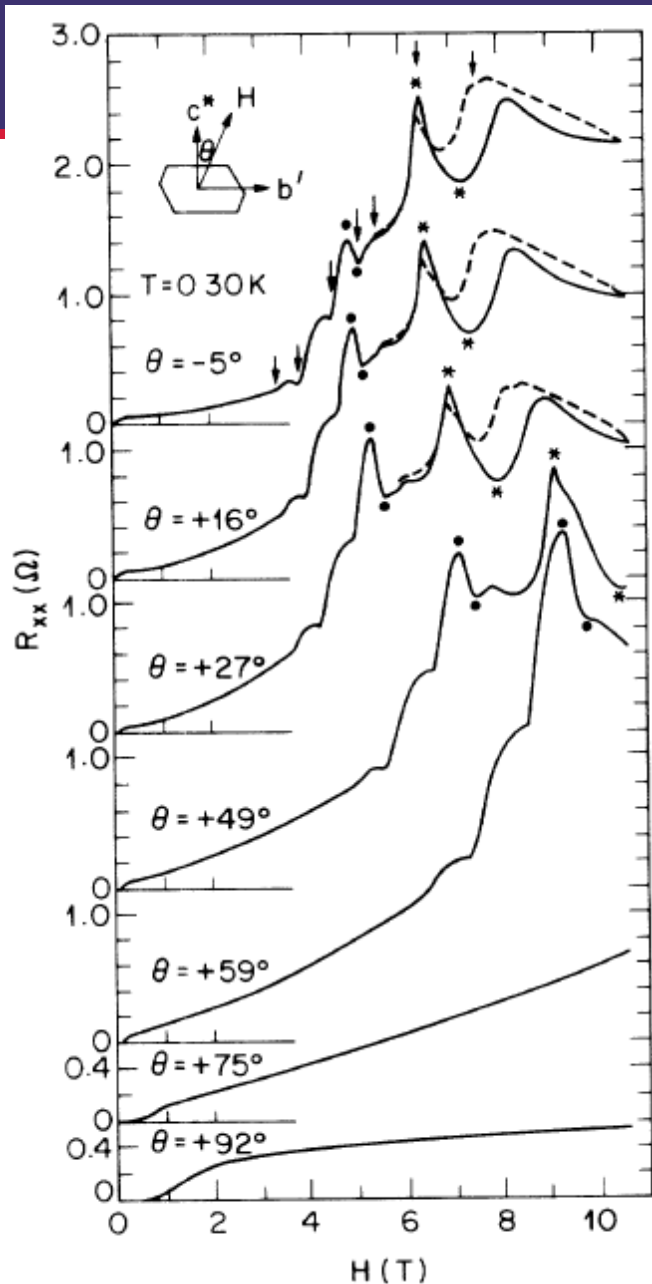


**Leonid's Story: Inspirational Lights in the Sky**





# We had interesting data in a Quasi-1D Metal



## Magnetic Field Induced Spin Density Wave Transitions in $(\text{TMTSF})_2\text{ClO}_4$ [later appeared in PRL 64, 591 (1990)]

L.P. Gor'kov and A.G. Lebed (1984)  
Motion in Real Space for Quasi-1D Electrons



## Anisotropy of an instability for a spin density wave induced by a magnetic field in a $Q1D$ conductor

A. G. Lebed'

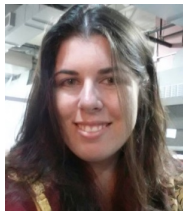
*L. D. Landau Institute of Theoretical Physics, Academy of Sciences of the USSR*

(Submitted 24 December 1985)

*Pis'ma Zh. Eksp. Teor. Fiz.* **43**, No. 3, 137-139 (10 February 1986)

The threshold field for the formation of a spin density wave in  $(\text{TMTSF})_2\text{X}$  compounds is shown to have an oscillatory anisotropy in the plane perpendicular to the chains,  $\mathbf{H} \perp \mathbf{a}$ . This field is at a minimum for the direction making an angle  $\varphi \approx 30^\circ$  with the  $c^*$  axis.

(Using High Magnetic Fields to Reveal...)  
Evidence of Critical Behavior  
near Optimum Doping  
in High-Temperature Superconductors



**Camilla M. Moir**, Scott Riggs, Jose Galvis,  
Paula Giraldo-Gallo, Xiujun Lian, Philip Walmsley,  
Jiun-Haw Chu, Ian R. Fisher, Arkady Shekhter, GSB

***"Multi-band mass enhancement towards a critical doping  
in a pnictide superconductor."***  $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$

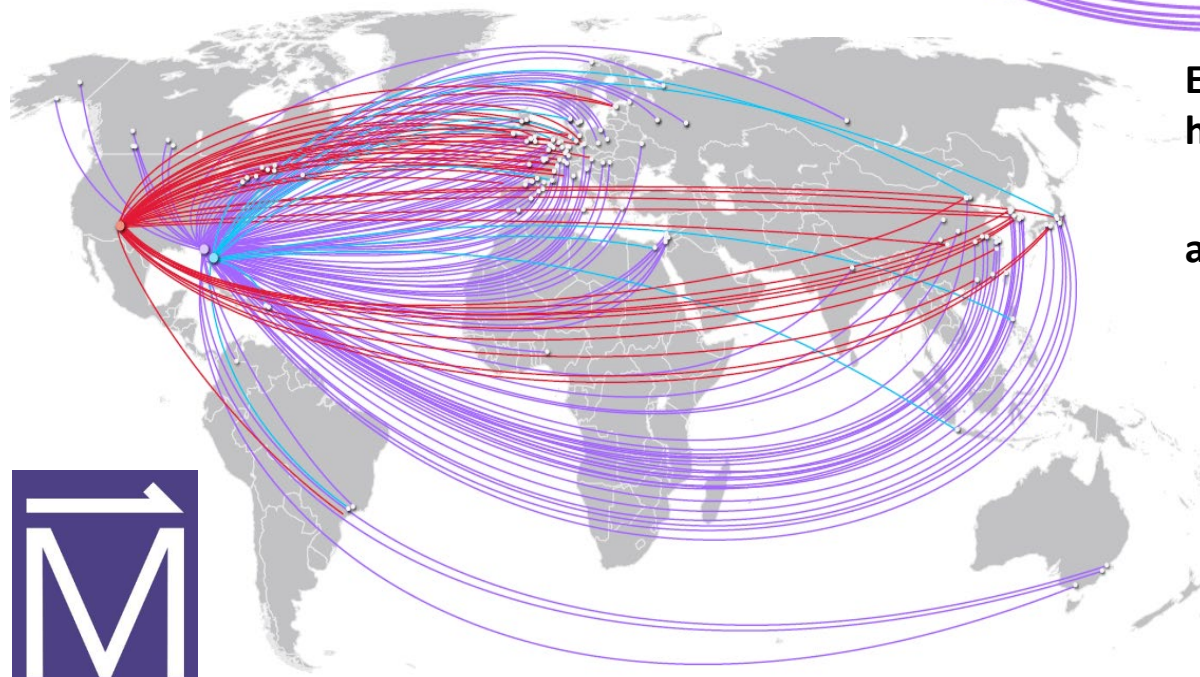
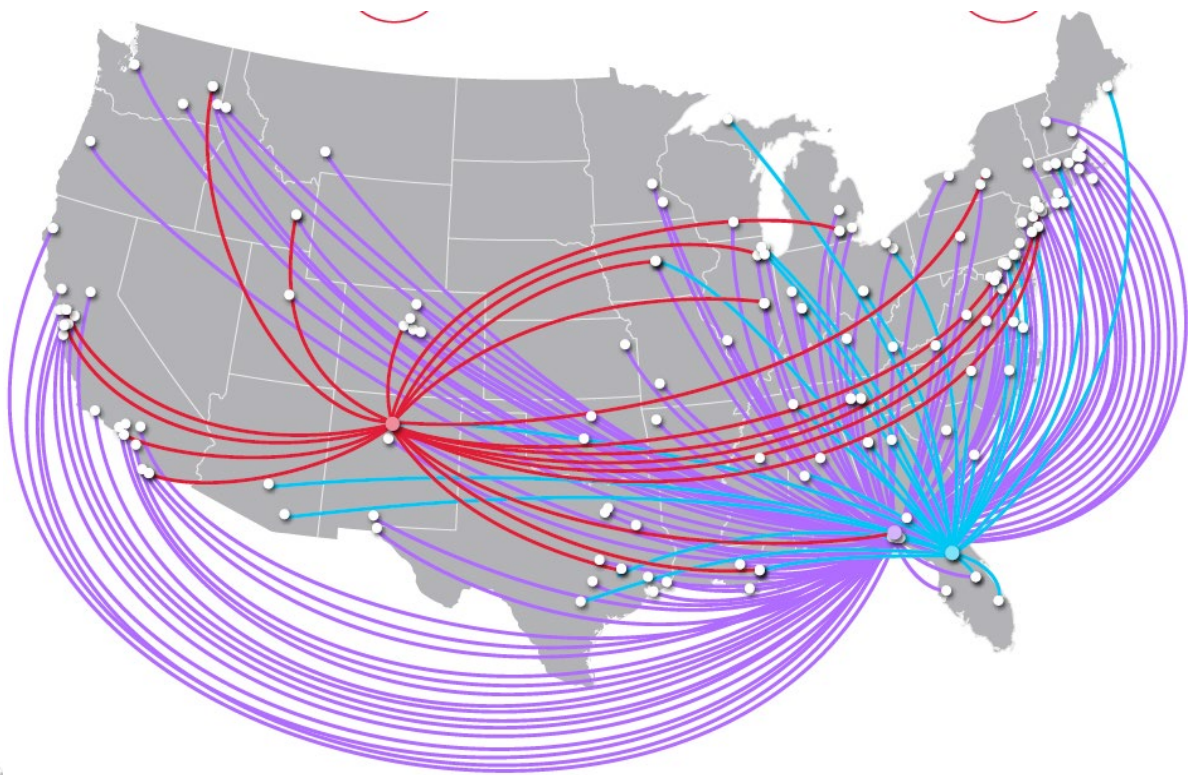
Nature Quantum Materials **4** (2019) DOI: 10.1038/s41535-018-0144-x.



# The MagLab attracts Researchers from Around The World

In 2018 alone, the MagLab hosted experiments by more than **2050 users** from **162 institutions** across the **United States**...

...and a total of **321 institutions** from throughout the world.



Every year...the MagLab User Program:  
helps to train **~225 postdocs**  
and **~560 graduate students**

and publishes **~450 refereed papers:**

- 6 *Proc. Nat'l Acad. Sciences*
- 24 *Nature Journals*
- 20 *Physical Review Letters*
- 62 *Physical Review B*
- 9 *J American Chemical Society*

**~ 25% of Principal Investigators are first-time-ever PI's at the MagLab**





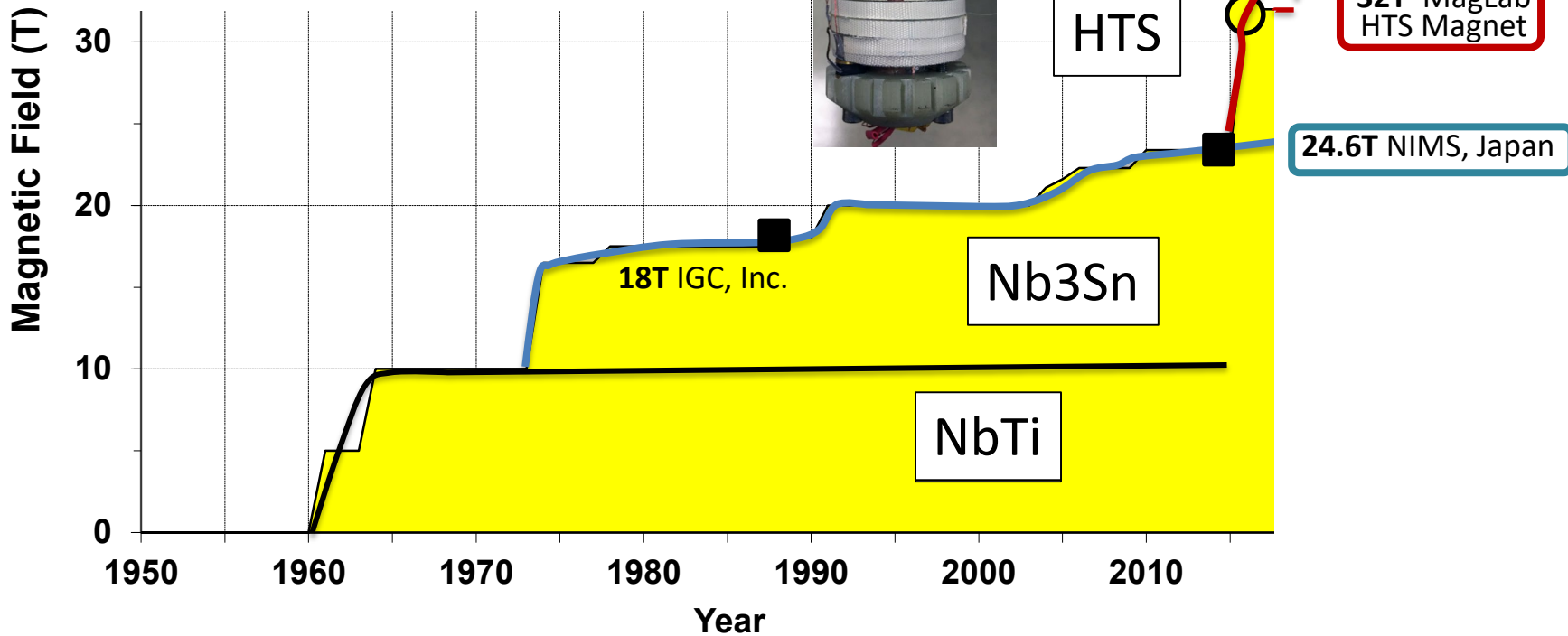
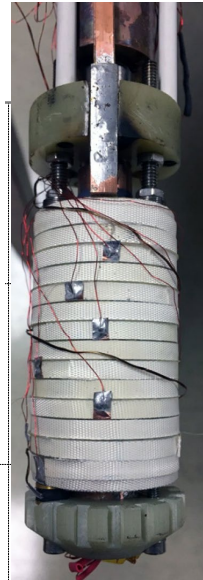
# Peak Fields for Superconducting Magnets

**nature**  
International journal of science

Letter | Published: 12 June 2019

## 45.5-tesla direct-current magnetic field generated with a high-temperature superconducting magnet

Seungyong Hahn, Kwanglok Kim, Kwangmin Kim, Xinbo Hu, Thomas Painter, Iain Dixon, Seokho Kim, Kabindra R. Bhattarai, So Noguchi, Jan Jaroszynski & David C. Larbalestier





# The Phase Diagram in 2001:

## Compilation of Evidence of a Quantum Phase Transition near Optimum Doping from High-Temperature Behaviors

J.L. Tallon, J.W. Loram, Physica C 349, 53 (2001)

*“The doping dependence of  $T^*$  - what is the real high- $T_c$  phase diagram?”*

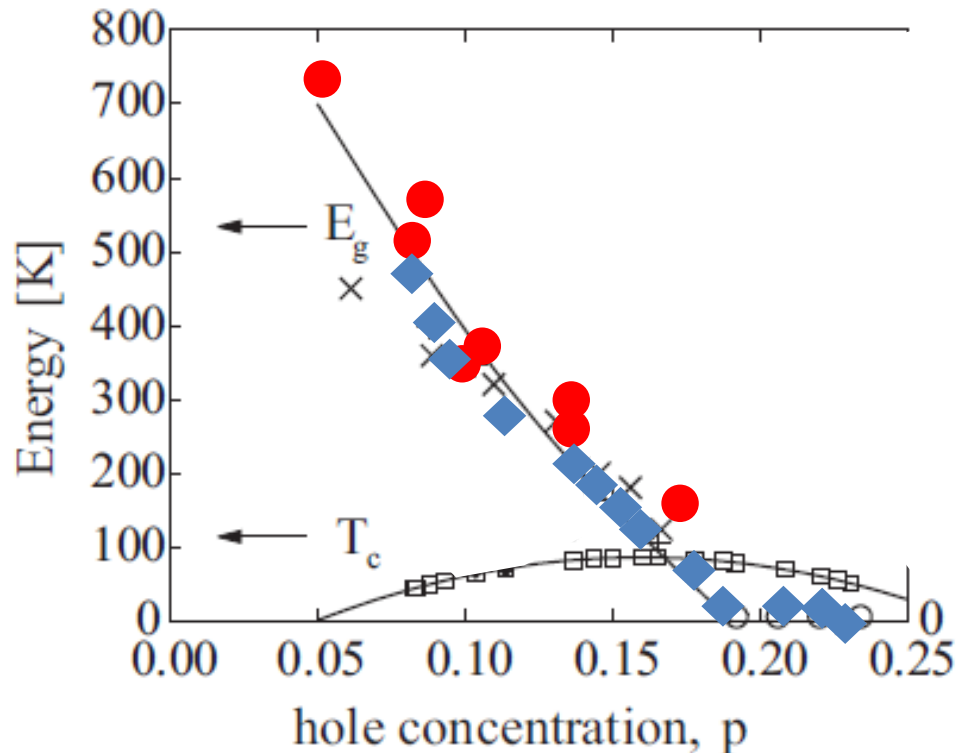
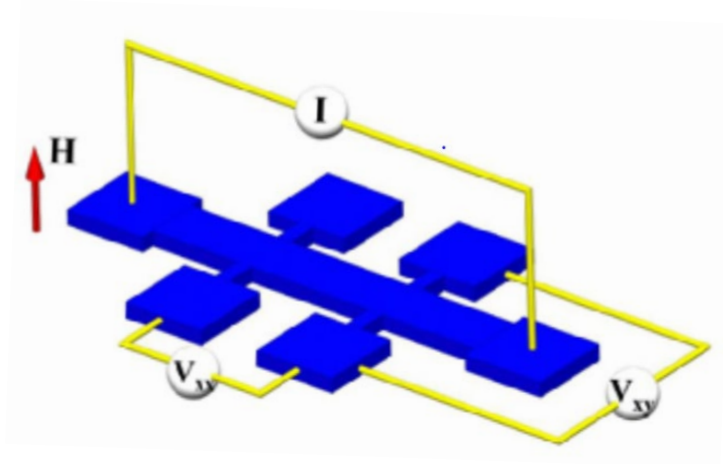


Fig. 4. The doping dependence of  $E_g$  for  $Y_{0.8}Ca_{0.2}Ba_2Cu_3O_{7-\delta}$  from  $^{89}K_s$  (●), from heat capacity (◆) jump at  $T_c$ , from the scaling of the resistivity (x), and the superconducting  $T_c$  (□).

**Using High Magnetic Fields  
to Evidence a Quantum Phase Transition  
near Optimum Doping  
in High Temperature Superconductors (LSCO and Bi-2201)**

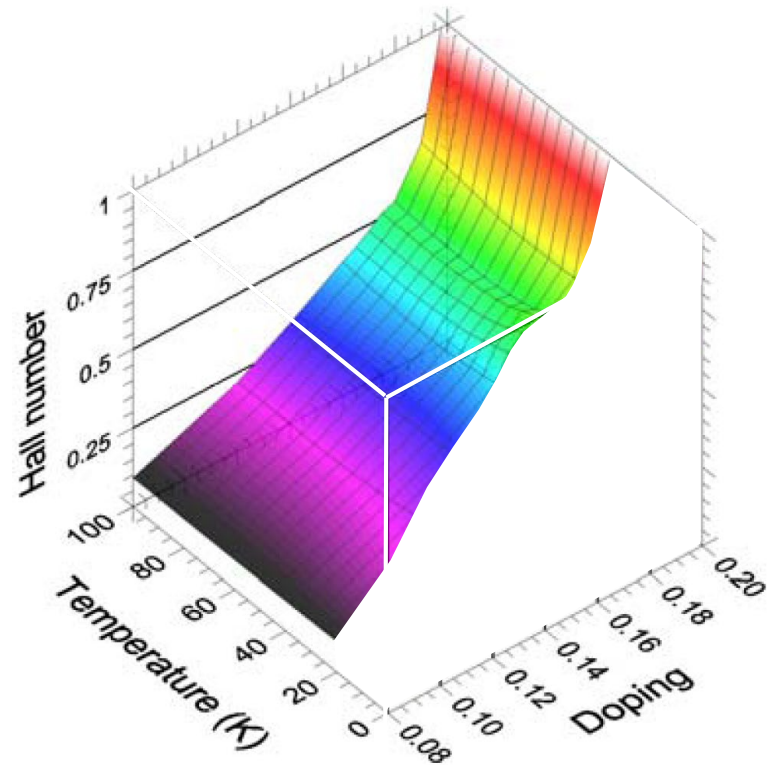
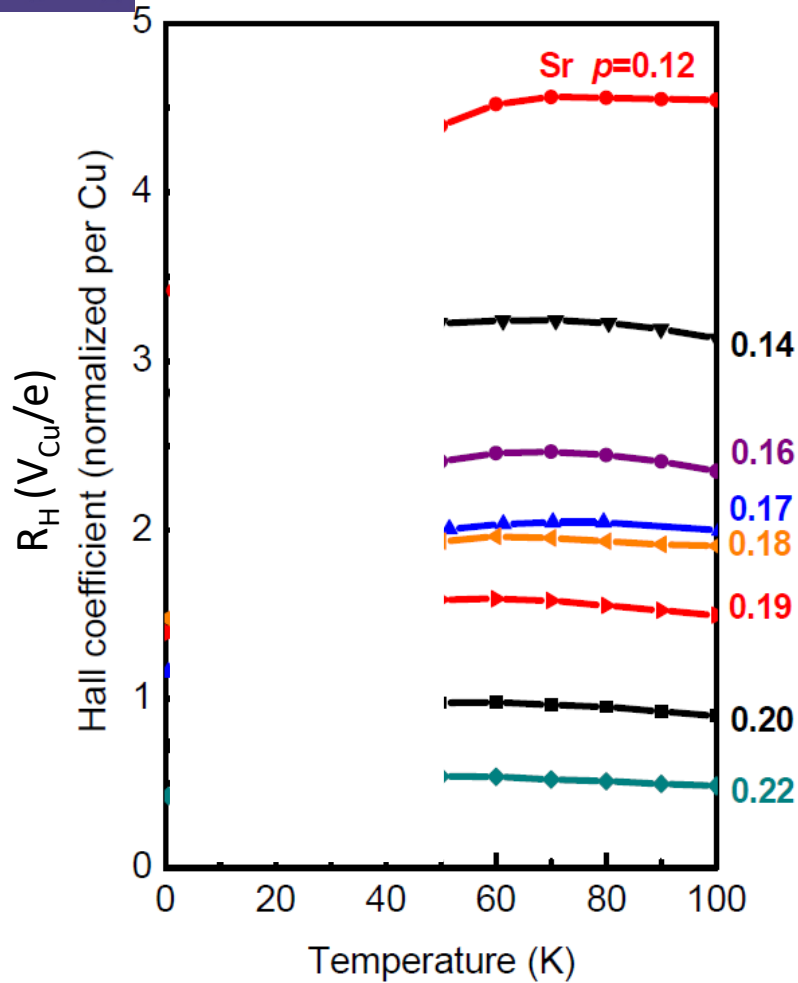


In a single band metal,  
 $V_{xy} / I = H/ne \equiv R_{\text{hall}} H$

↖ “Hall number”

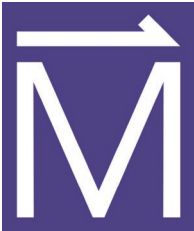


# The Hall Coefficient, $R_H$ , of the Normal State of LSCO in the Zero-Temperature Limit

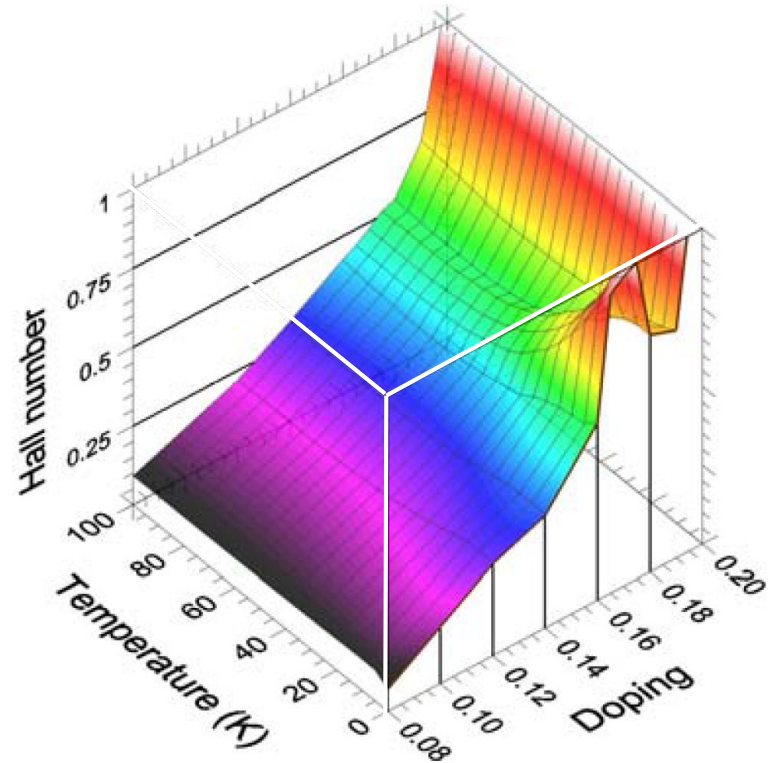
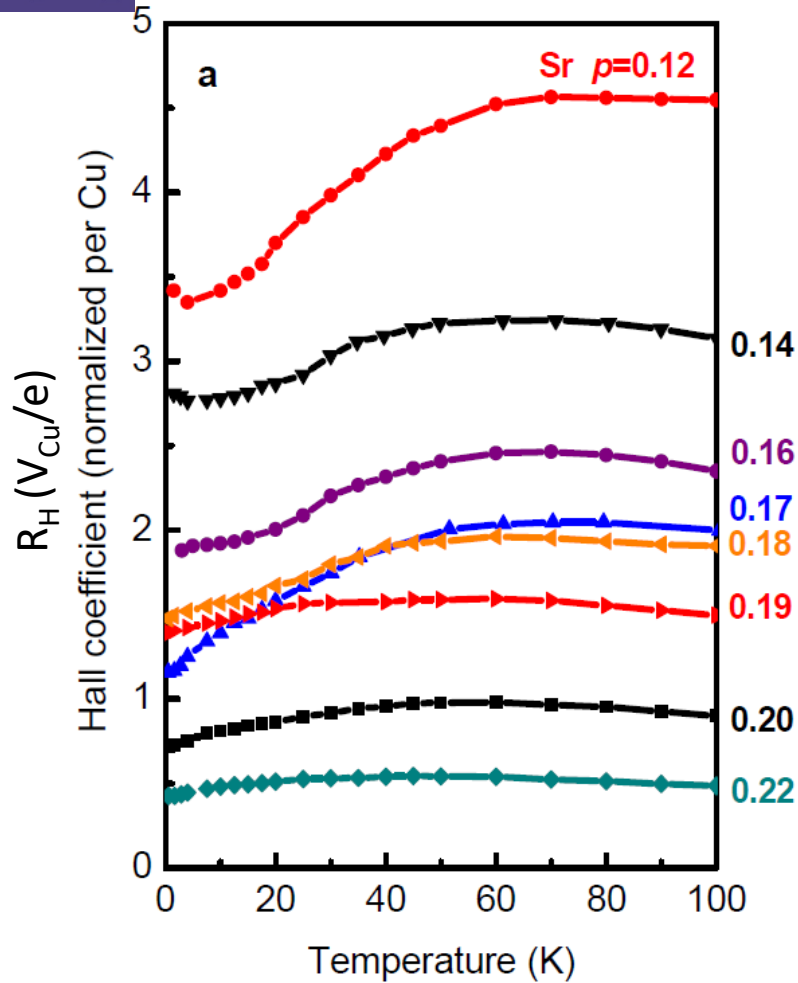


F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger,  
Phys.Rev.Lett. 102, 017004 (2009).

*“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”*

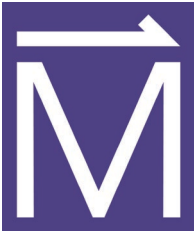


# The Hall Coefficient, $R_H$ , of the Normal State of LSCO in the Zero-Temperature Limit

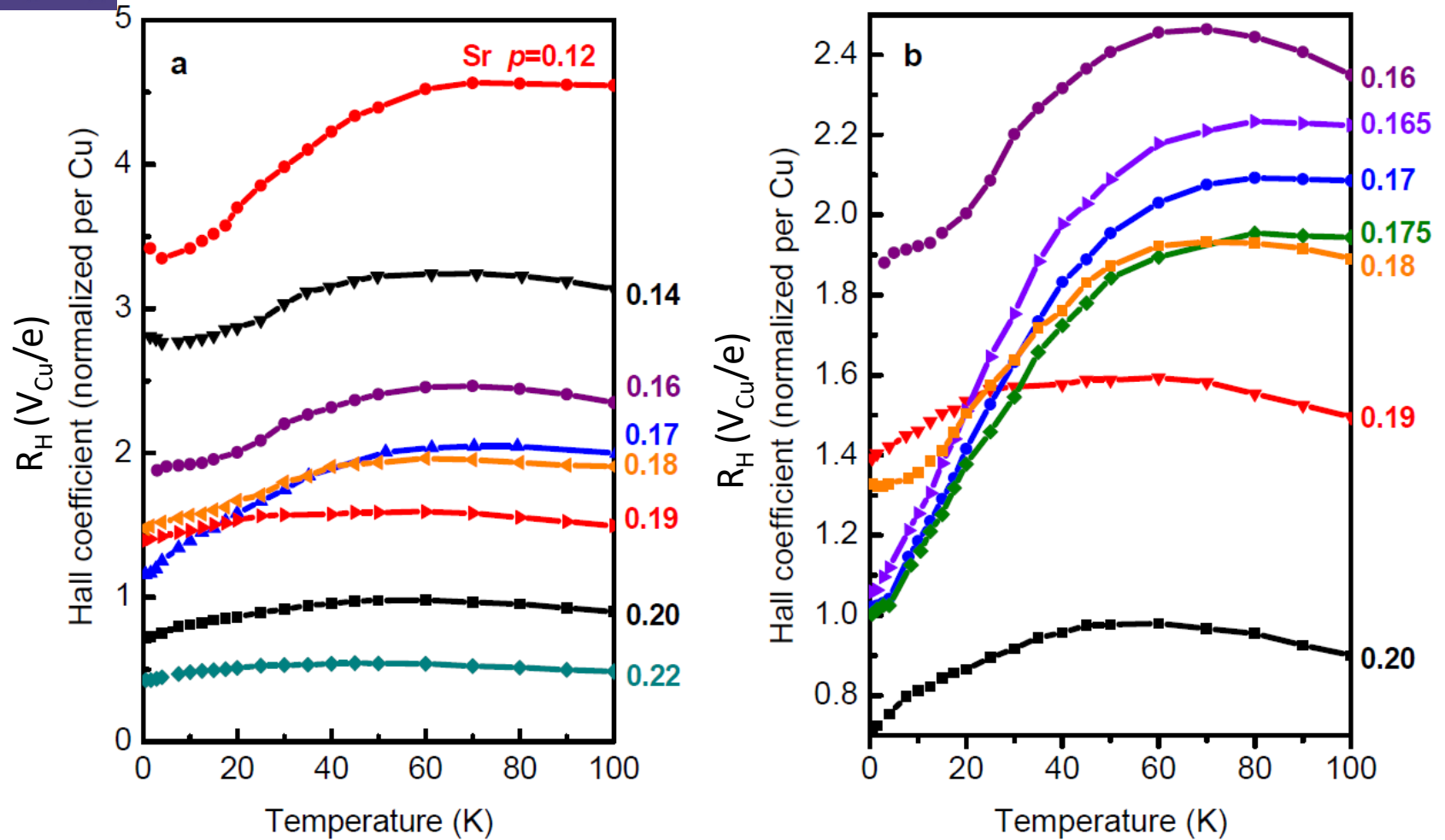


F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger,  
Phys.Rev.Lett. 102, 017004 (2009).

“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”



# The Hall Coefficient, $R_H$ , in the Normal State of LSCO in the Zero-Temperature Limit

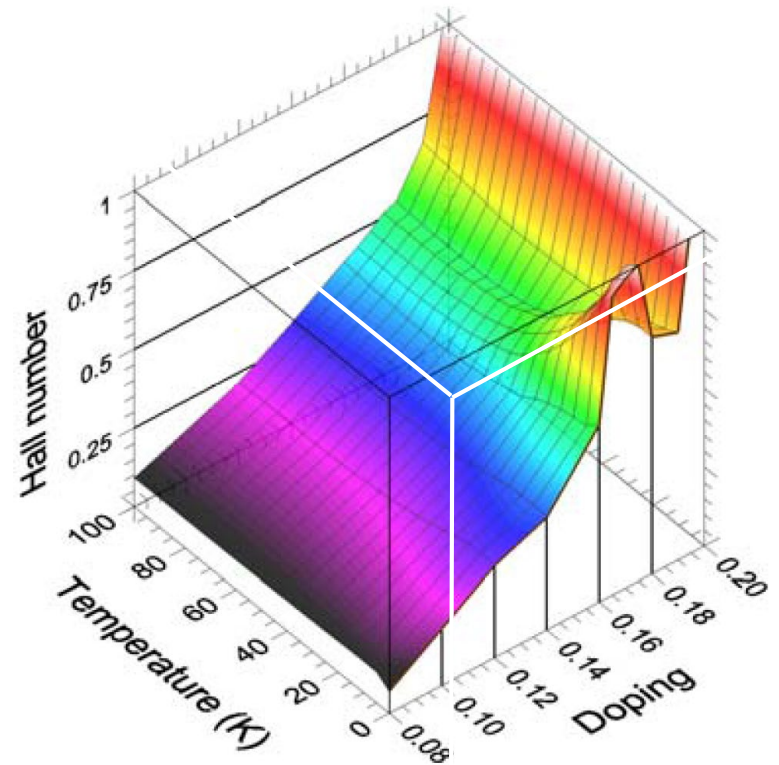
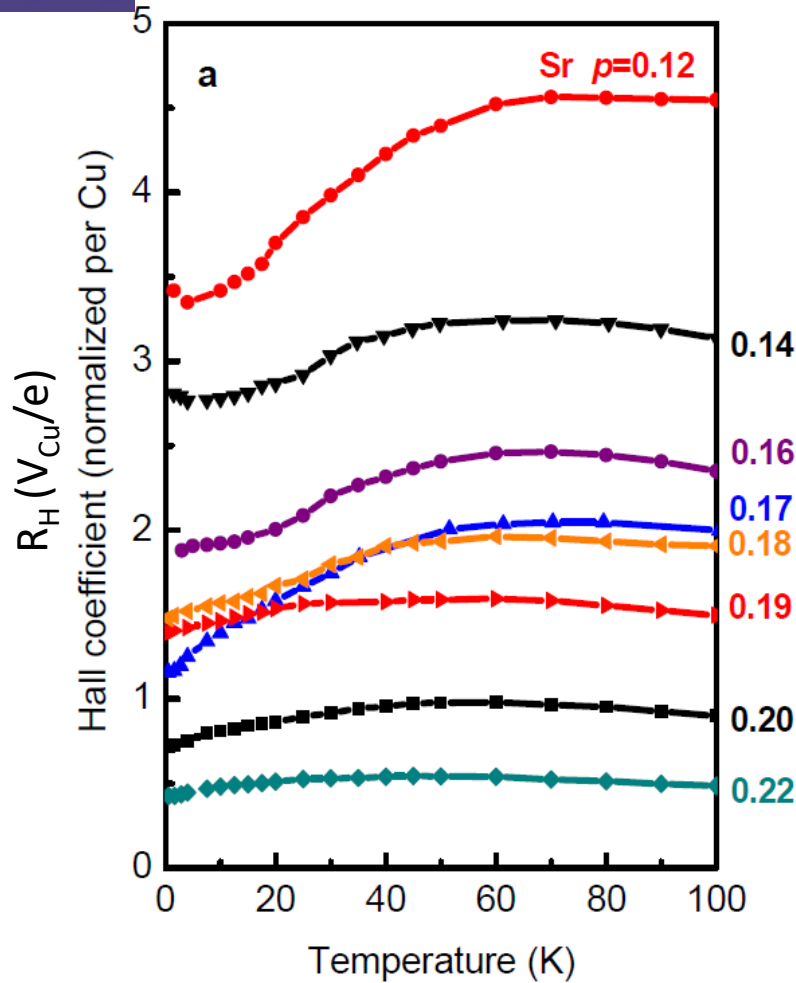


F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger,  
Phys.Rev.Lett. 102, 017004 (2009).

*“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”*

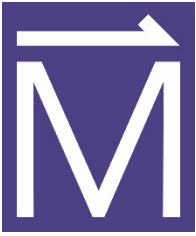


# The Hall Coefficient, $R_H$ , of the Normal State of LSCO in the Zero-Temperature Limit



F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger, Phys.Rev.Lett. 102, 017004 (2009).

*“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”*



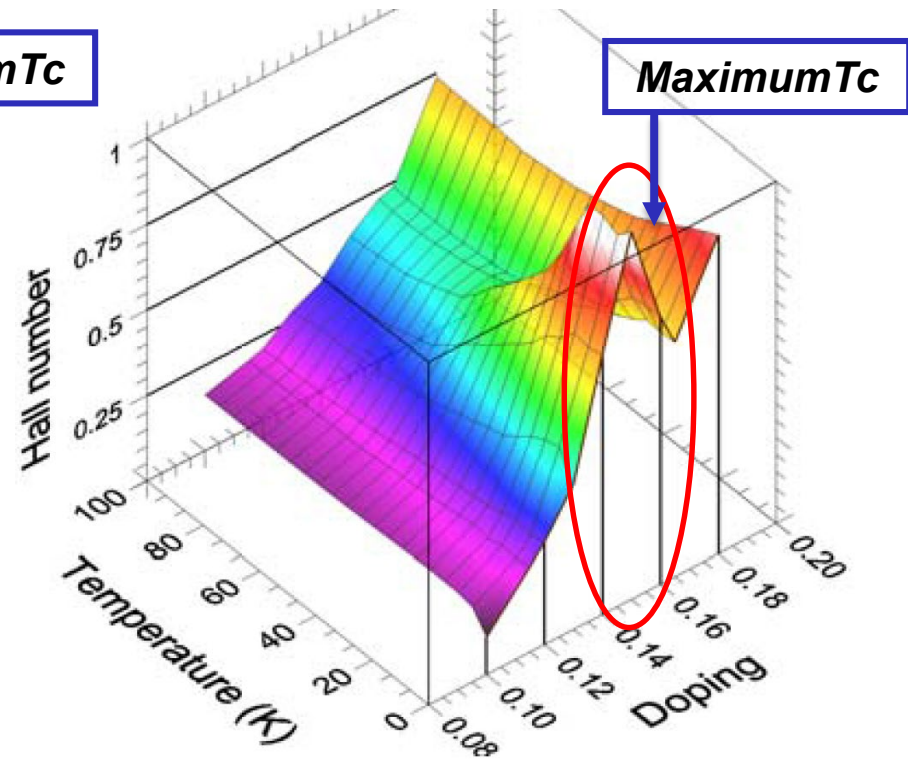
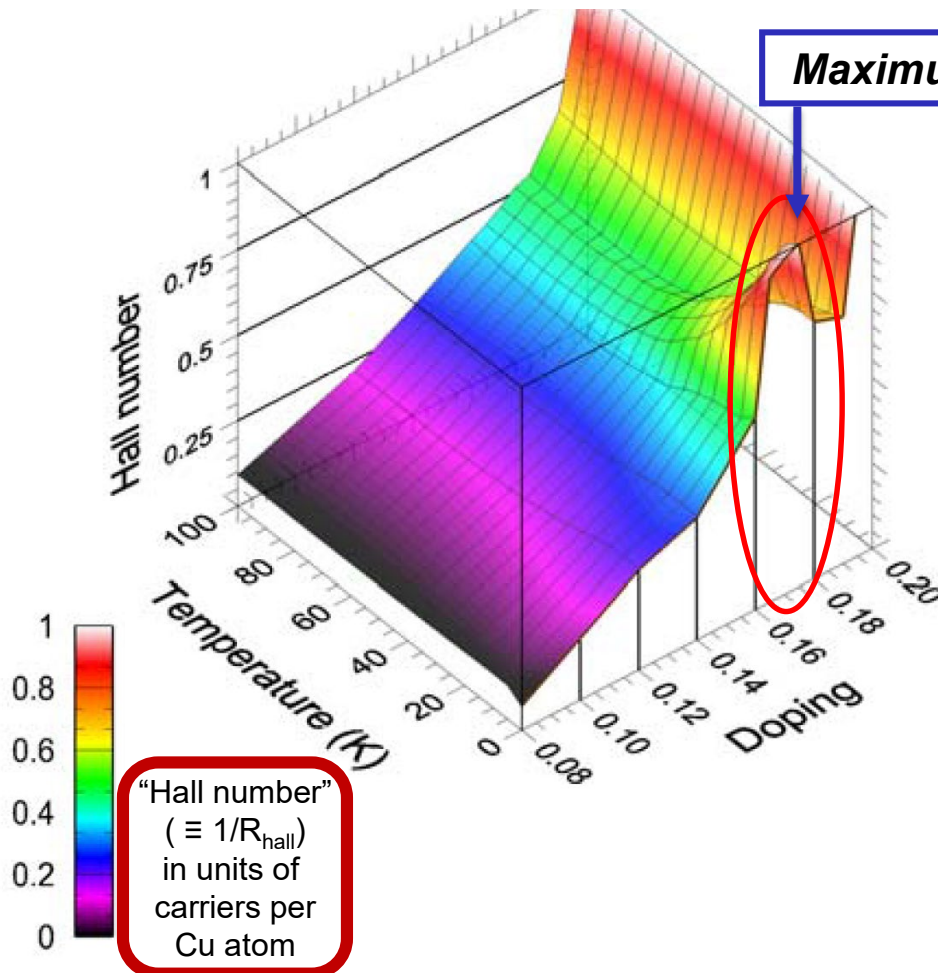
# Peak in Hall Number near Optimum $T_c$ seen in two systems

Reported in LSCO thin films in 2009...

F. F. Balakirev, J. B. Betts, A. Migliori, I. Tsukada, Yoichi Ando, G. S. Boebinger, *Phys.Rev.Lett.* 102, 017004 (2009).  
“Quantum Phase Transition in the Normal State of High- $T_c$  Cuprates at Optimum Doping.”

...but first observed in Bi-2201 single crystals in 2003

Fedor F. Balakirev, Jonathan B. Betts, Albert Migliori, S. Ono, Yoichi Ando & Gregory S. Boebinger, *Nature* 424, 912 (2003).  
“Signature of optimal doping in Hall-effect measurements on a high-temperature superconductor”

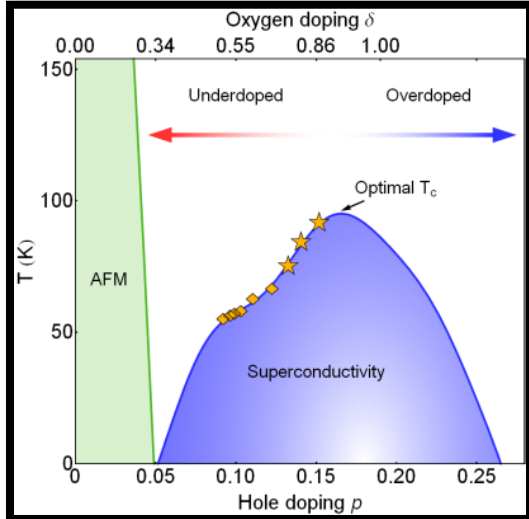


**Using High Magnetic Fields  
to Evidence Quantum Criticality  
near Optimum Doping  
in a High Temperature Superconductor  
(Ramshaw, et al. in YBCO)**



# A Quantum Critical Point at the Heart of High-Temperature Superconductivity in YBCO

B. Ramshaw, S.E. Sebastian, R.D. McDonald, James Day, B. Tan, Z. Zhu, J.B. Betts, Ruixing Liang, D.A. Bonn, W.N. Hardy, N. Harrison  
 Science (2015) DOI: 10.1126/science.aaa4990

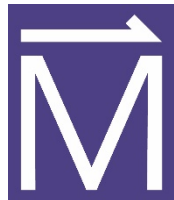
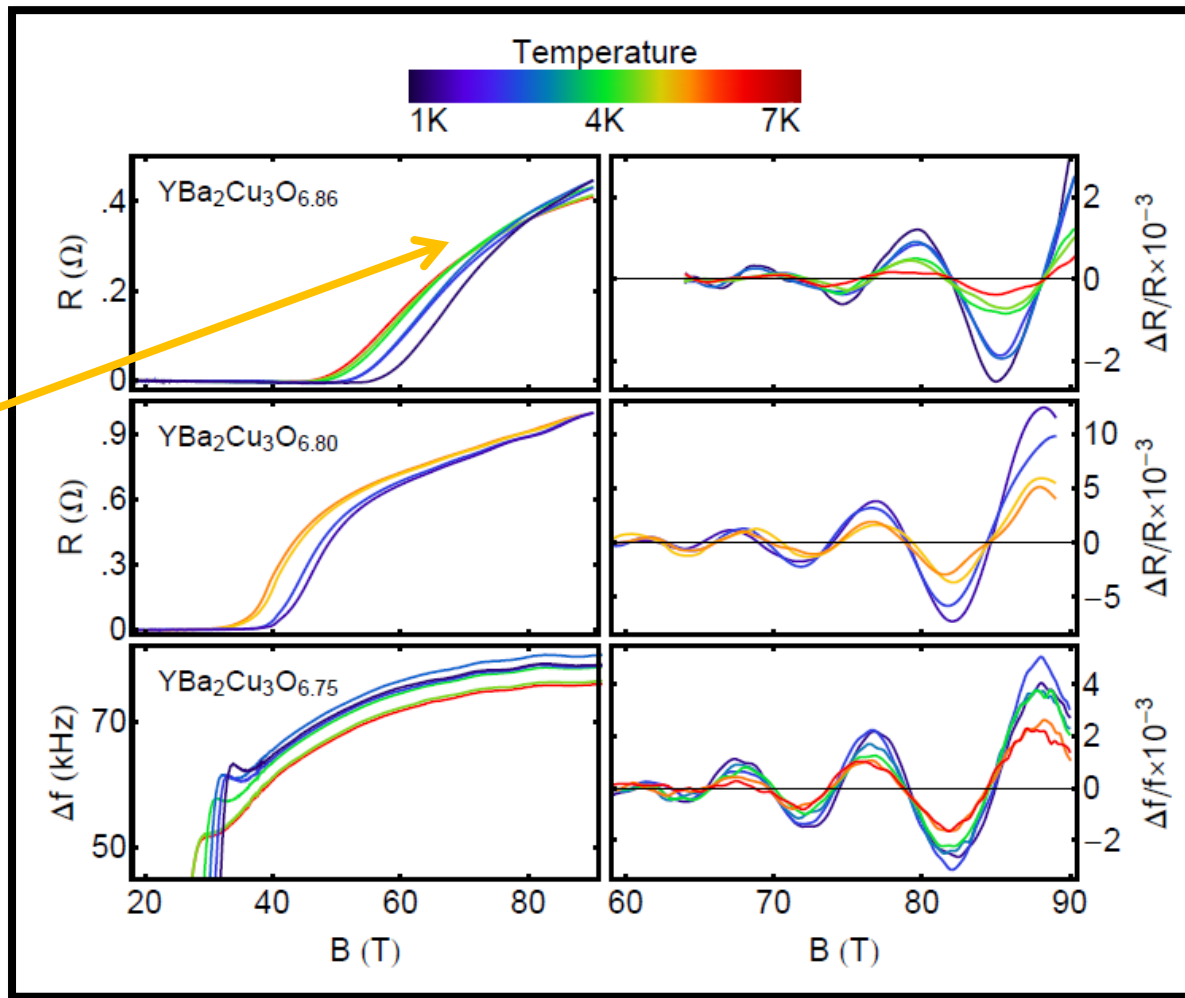


$T_c \sim 91\text{K}$

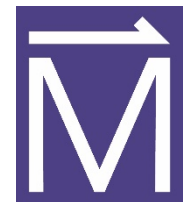
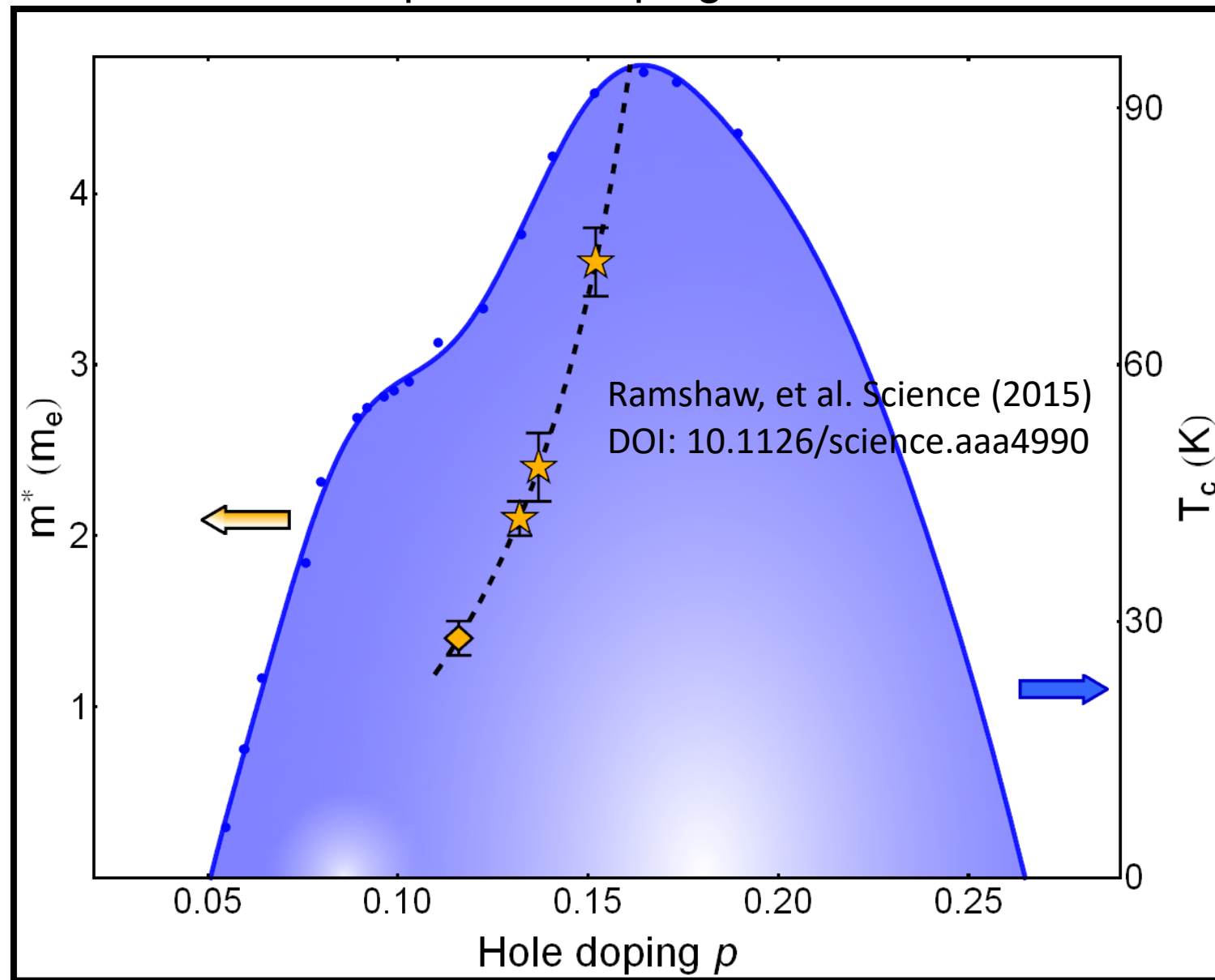
**CLEARLY:** We Need Bigger Magnets!

$T_c \sim 81\text{K}$

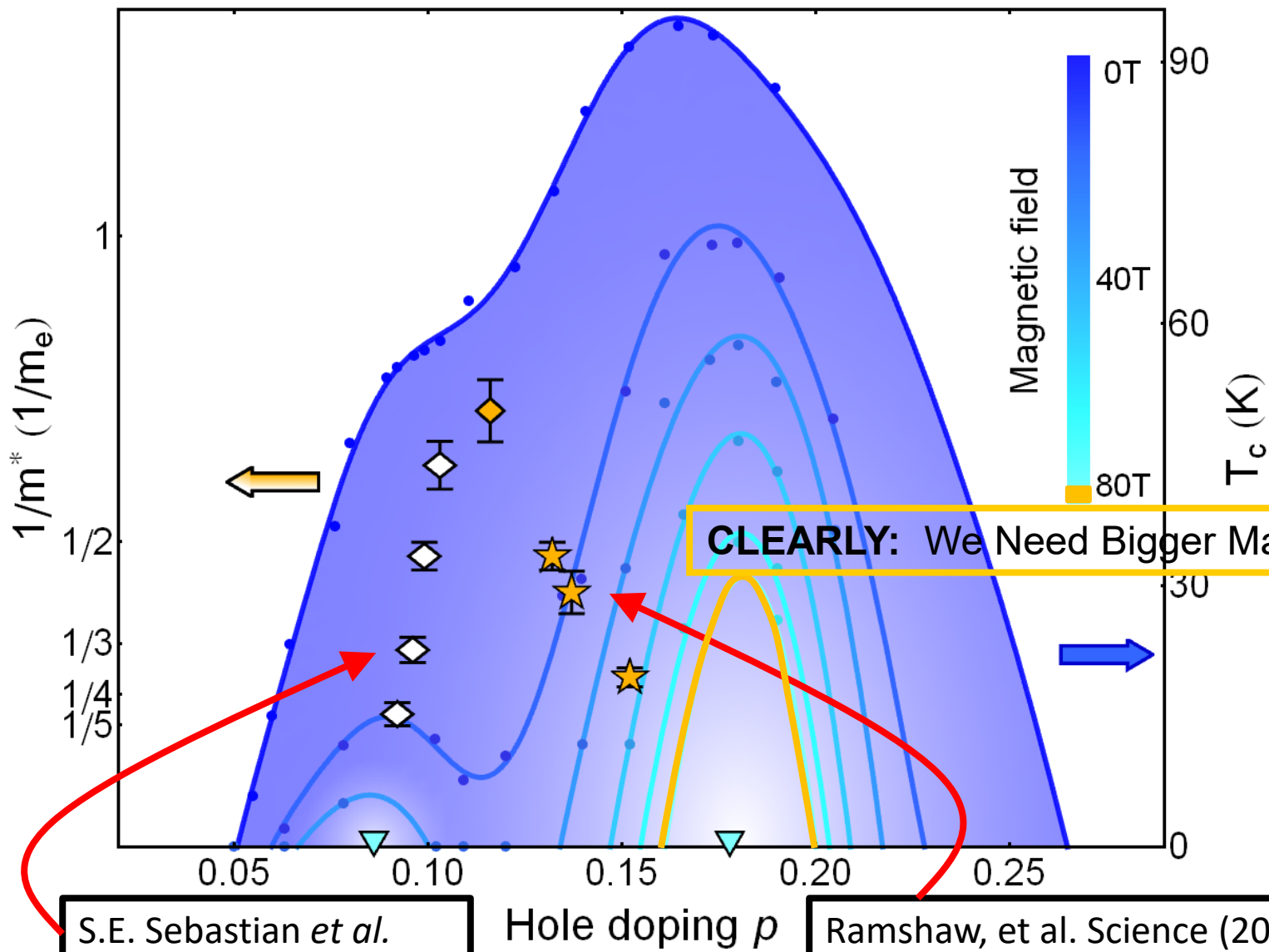
$T_c \sim 75\text{K}$



# Diverging Effective Mass: Evidence of a Quantum Critical Point at Optimum Doping in YBCO



# Diverging Effective Mass: Evidence of a Quantum Critical Point at Optimum Doping in YBCO



S.E. Sebastian *et al.*  
PNAS **107**, 6175 (2010)

Hole doping  $p$

Ramshaw, et al. Science (2015)  
DOI: 10.1126/science.aaa4990

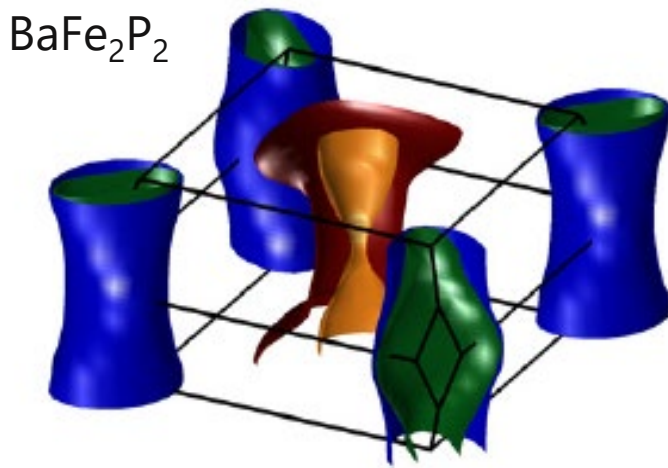
**Turn to the Ba122 Iron Pnictide Superconductor  
(which has a lower Upper Critical Magnetic Field)**

**To Use Specific Heat in High Magnetic Fields  
to reveal Thermodynamic Evidence  
of a Quasiparticle Mass Divergence  
at Optimum Doping**

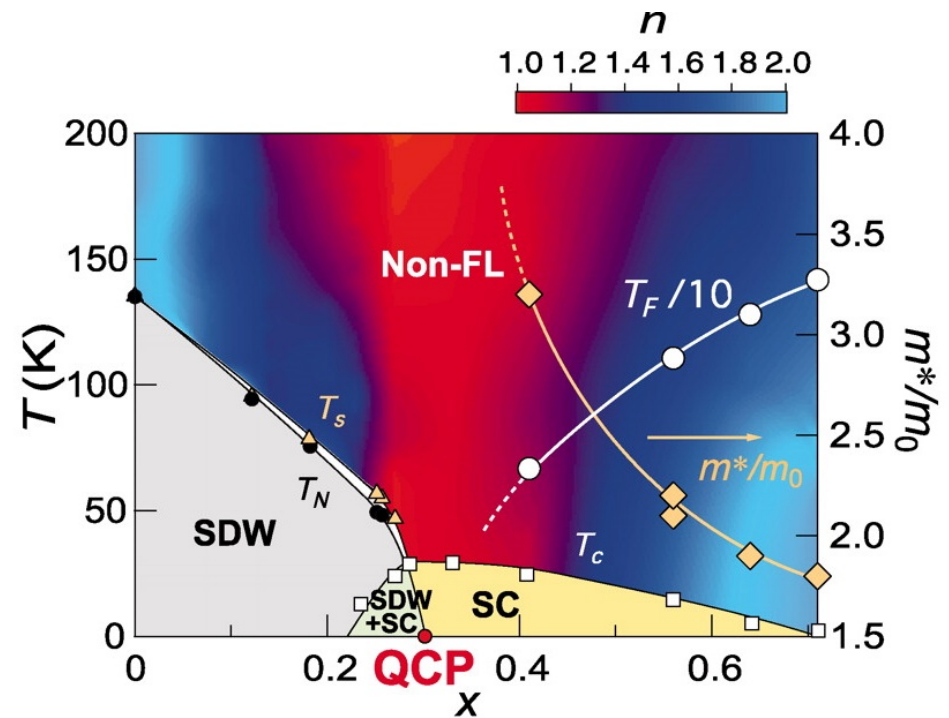
# BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>



- Quasi 2D Fermi surface with multiple pockets
- Isovalent P-substitution maps out a familiar-looking phase diagram
- Non-Fermi-Liquid phase exhibiting linear-in-T resistivity
- Is there a Quantum Critical Point near optimal doping?



A. Carrington, *et al.*  
*Rep. Prog. Phys.* **74**, 124507 (2011)



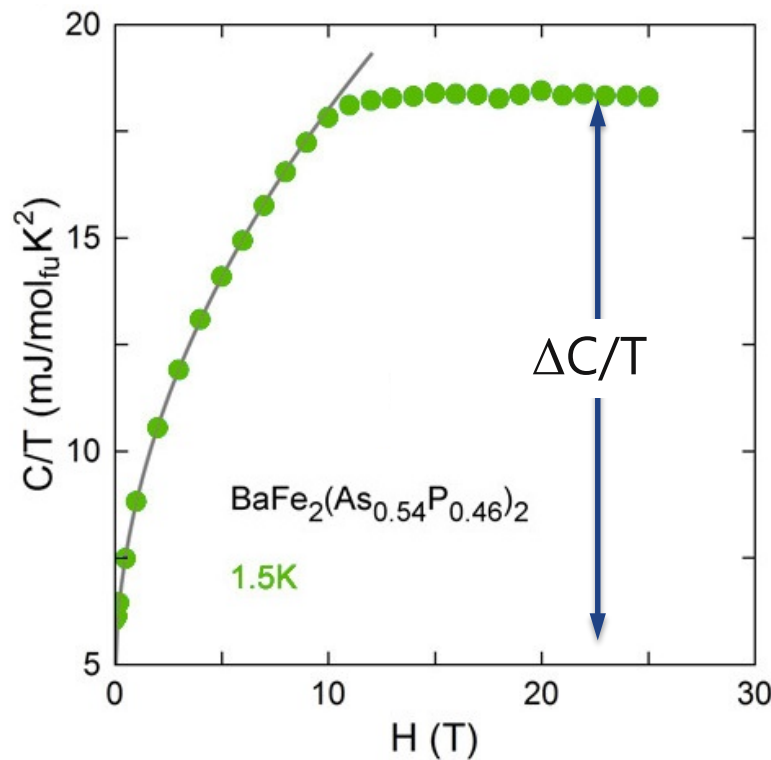
K. Hashimoto *et al.* *Science* 2012; **336**:1554-1557  
[*m\** data from quantum oscillations by H. Shishido *et al.*  
*Phys. Rev. Lett.* 2010; **104**:057008]

# Our Specific Heat Measurements



## Heat Capacity as a Function of Magnetic Field

- Sufficiently high magnetic fields (35T) to suppress superconductivity
- For us,  $\Delta C/T$  is the specific heat recovered by suppressing superconductivity



35 T resistive magnet at the National High Magnetic Field Laboratory

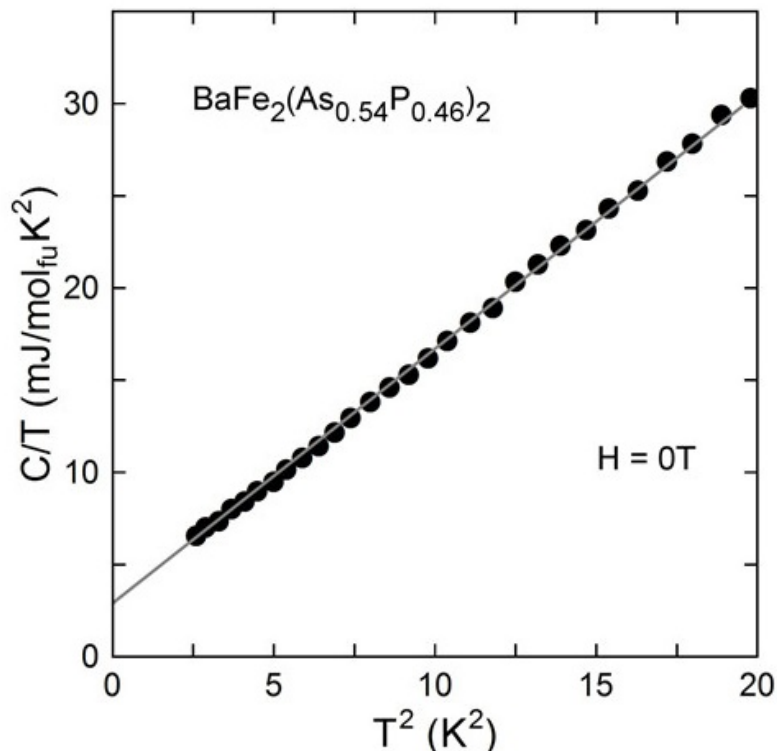


# Our Data

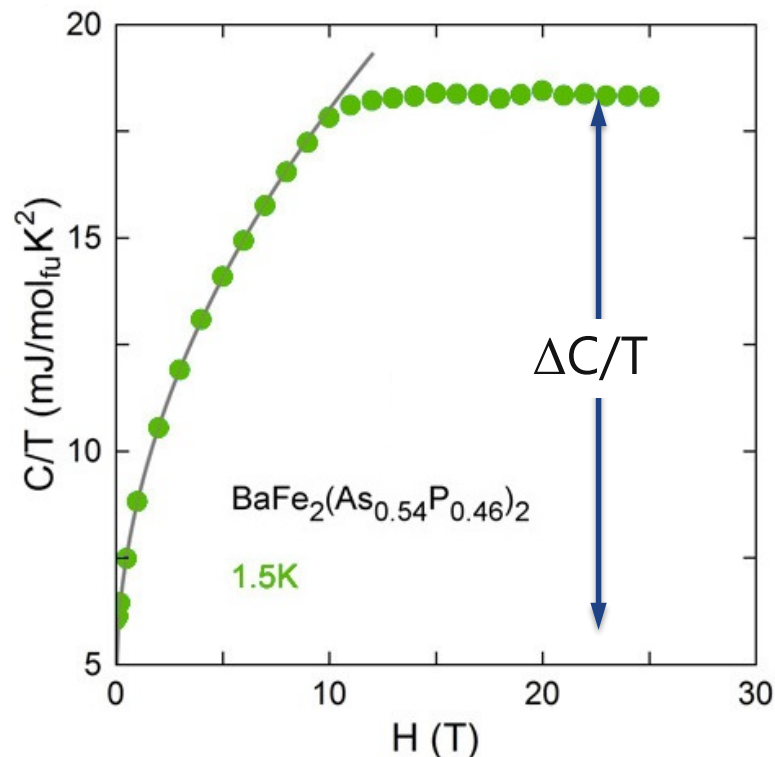
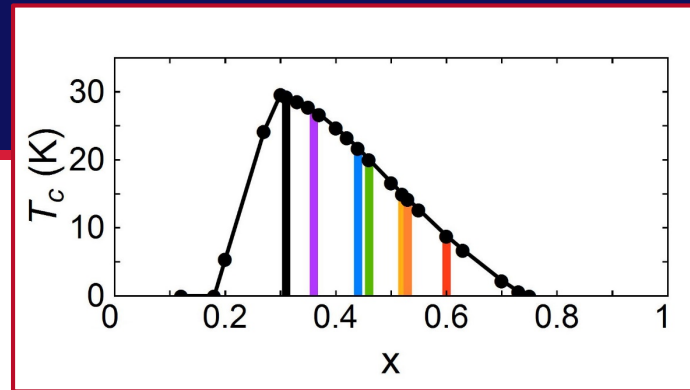
Moir, C.M. *et al.*  
*arXiv:1608.07510* (2016)

## Heat Capacity as a Function of

- Temperature
- Magnetic Field



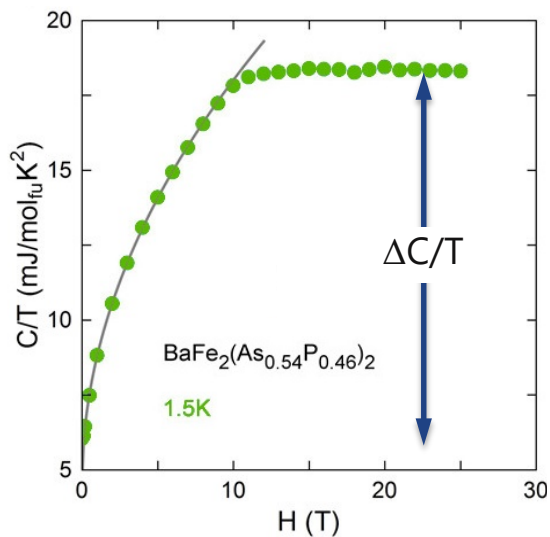
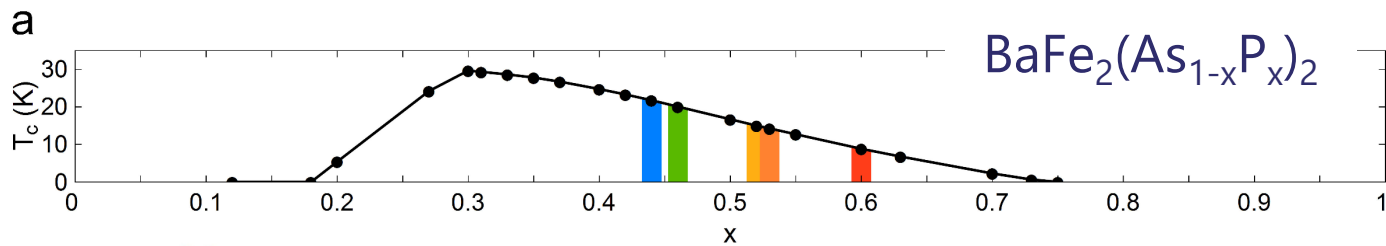
Temperature dependence shows finite  $C/T$  at  $H = 0, T = 0$ .



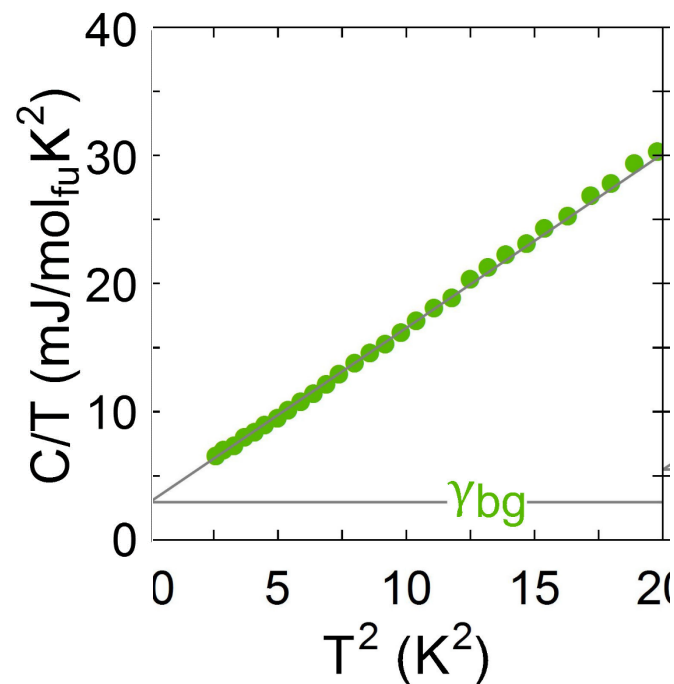
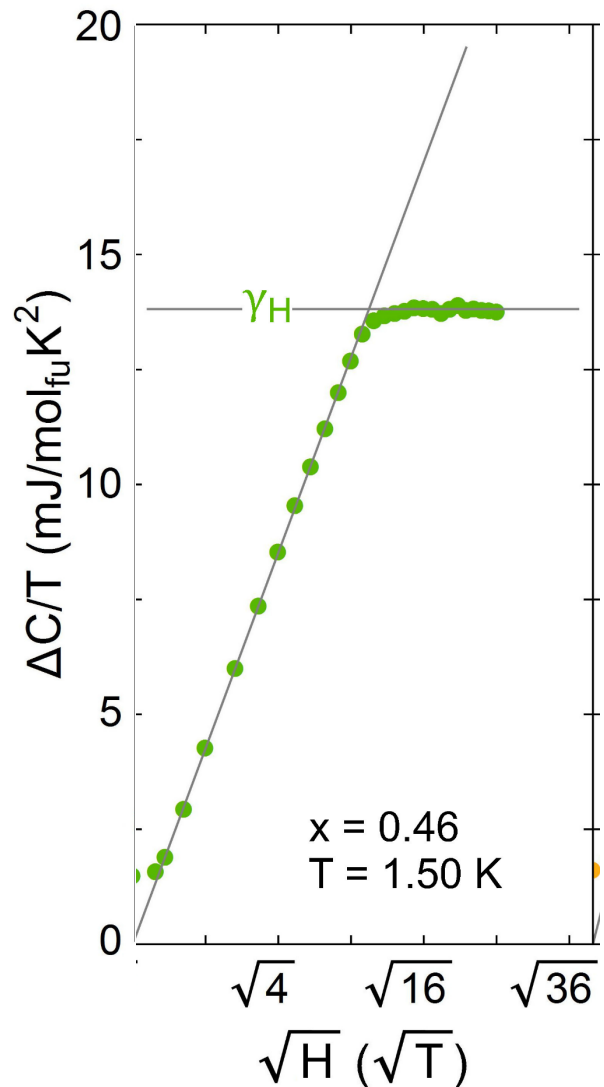
$\sqrt{H}$  dependence indicates line nodes in the superconducting gap.

C.M. Moir, *et al.*

***Nature Quantum Mat'l*** (2019)



$$\Delta C/T \rightarrow \gamma_H$$

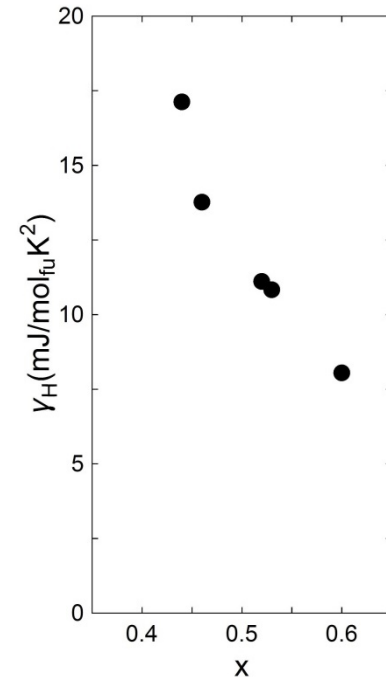
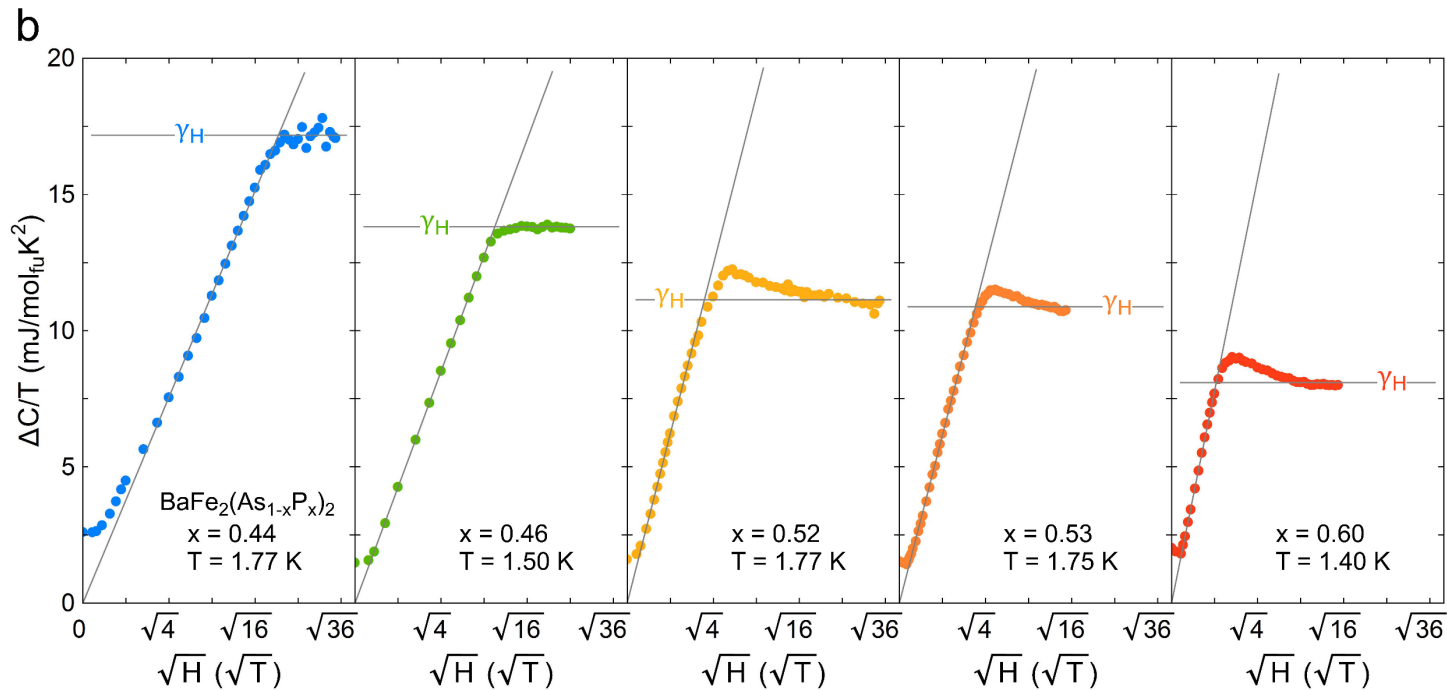
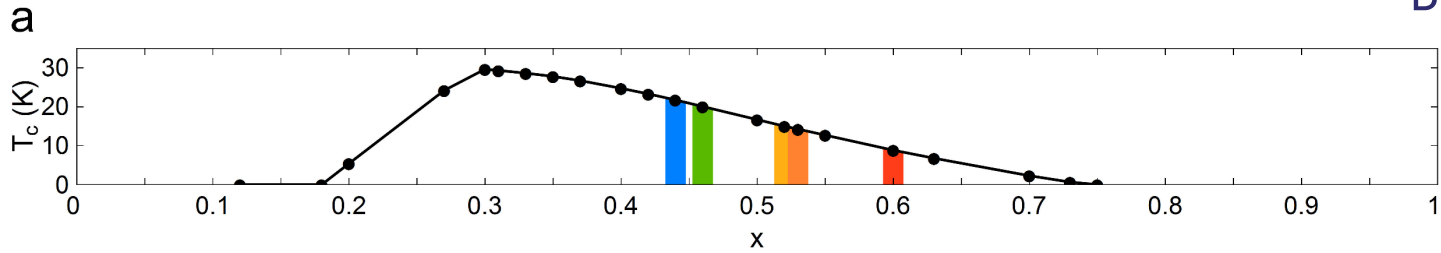






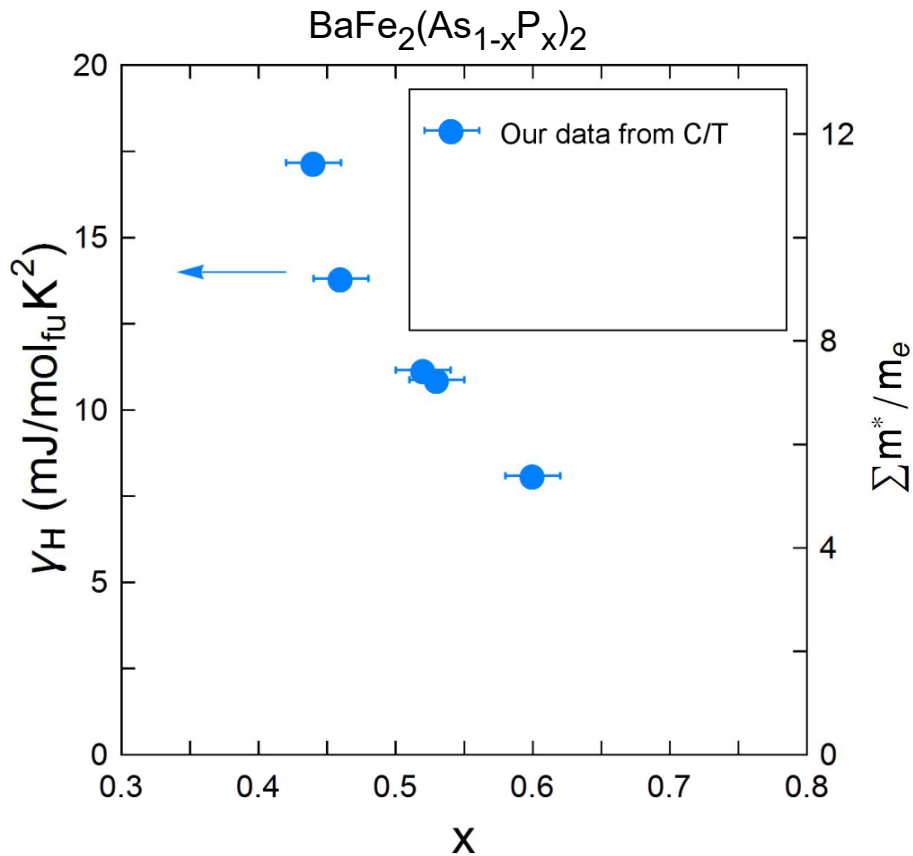
# Doping Dependence of $\gamma_H$

$\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$



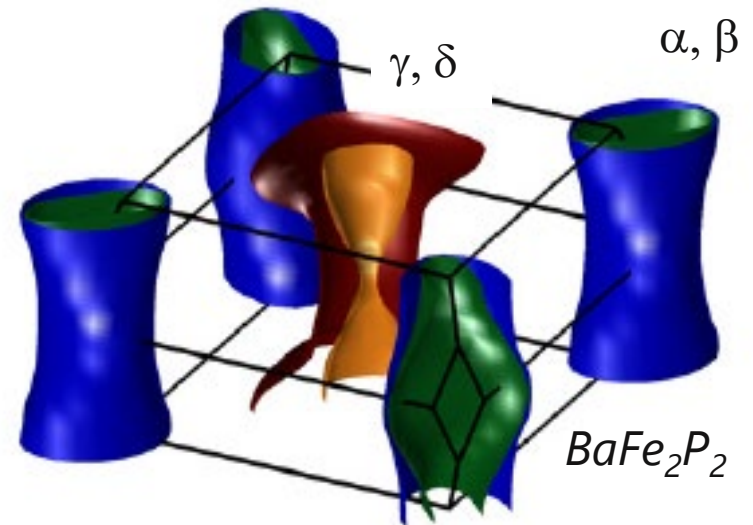


# Interpreting Enhancement of $\gamma_H$ as a Quasiparticle Mass Enhancement



In our units, for the warped cylindrical Fermi surfaces of Ba122,

$$\gamma = 1.5 \sum n_i m_i.$$



...for all pockets that take part in superconductivity

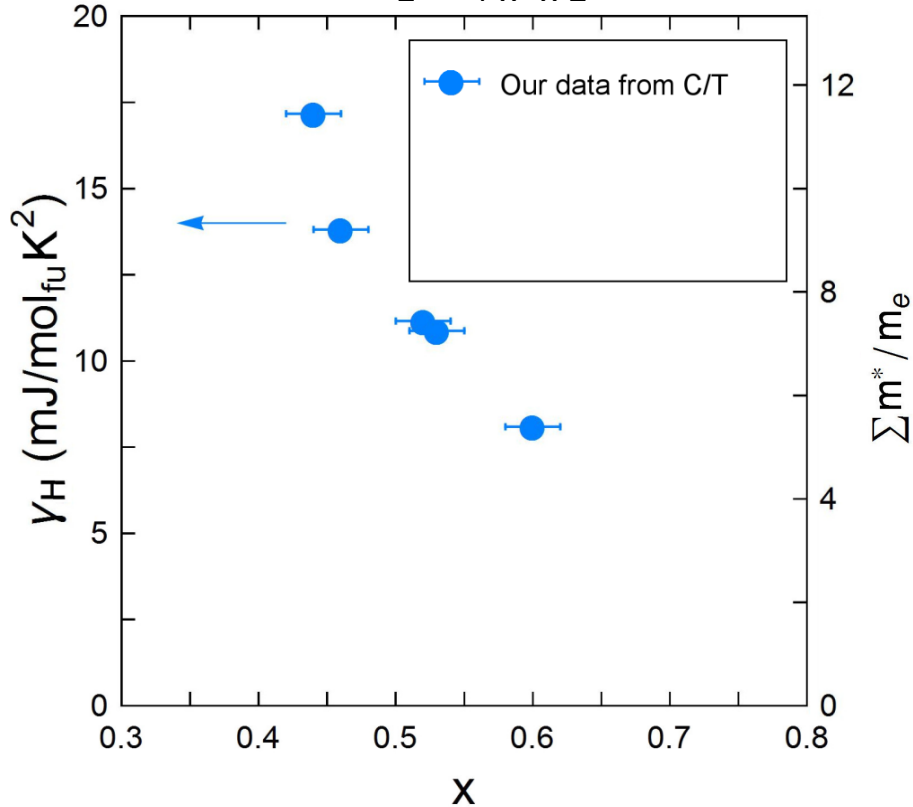
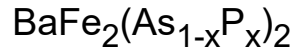
...independent of whether a given pocket shows quantum oscillations.

C.M. Moir, et al.

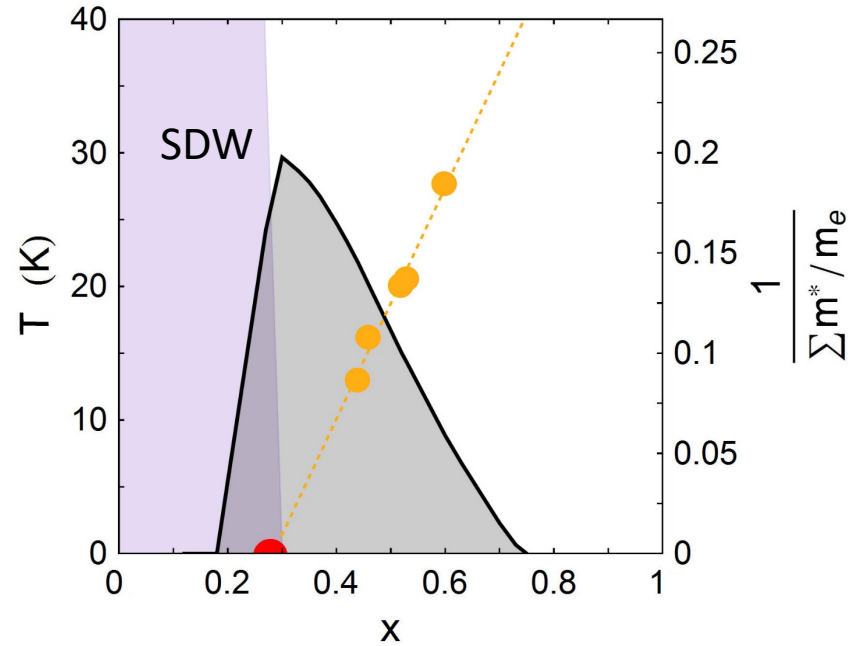
**Nature Quantum Mat'l (2019)**



# Mass Enhancement Appears to Diverge at Optimum Doping



$$\gamma = 1.5 \sum n_i m_i$$



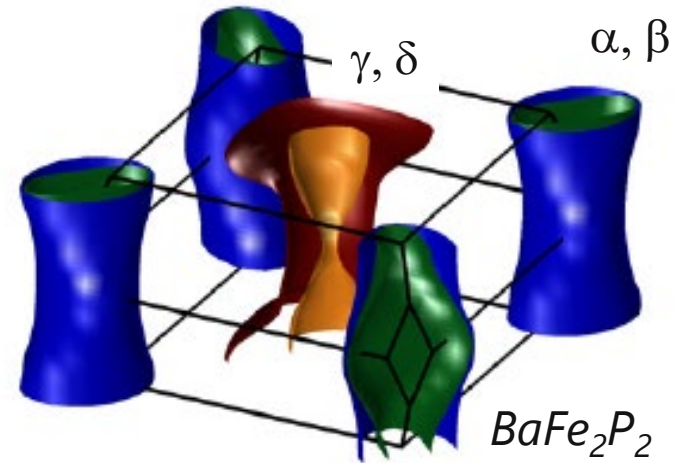
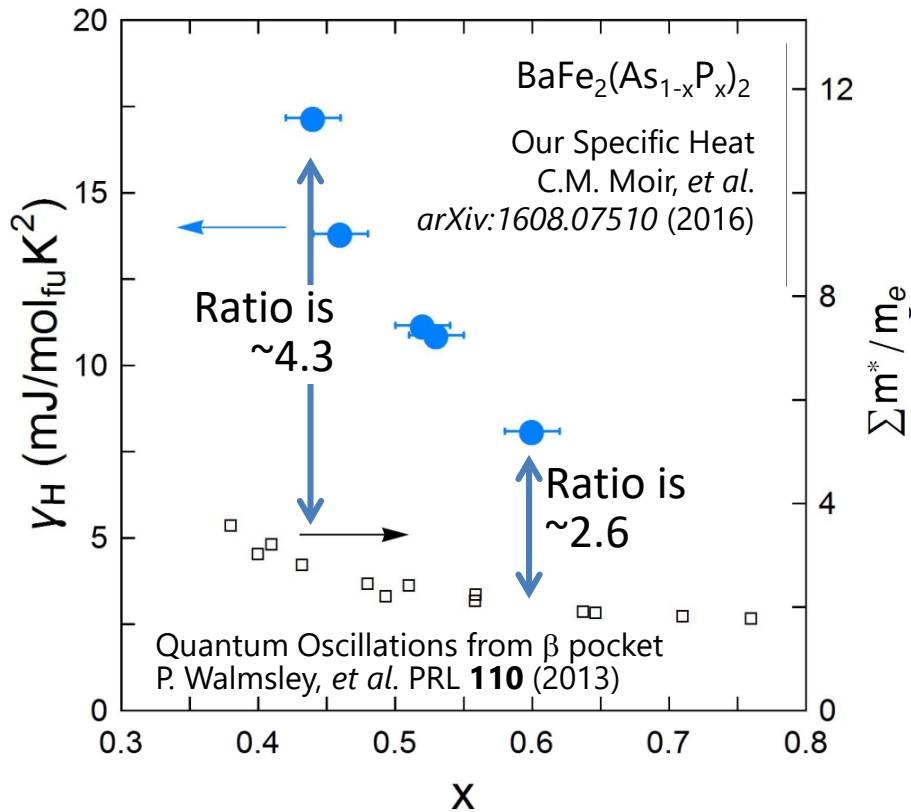
Linear fit to  $1/\Sigma m^* m_e$  extrapolates to zero near optimal doping at  $x=0.31$

C.M. Moir, et al.

**Nature Quantum Mat'l (2019)**



# Comparison of Mass Enhancement: Specific Heat and Quantum Oscillations



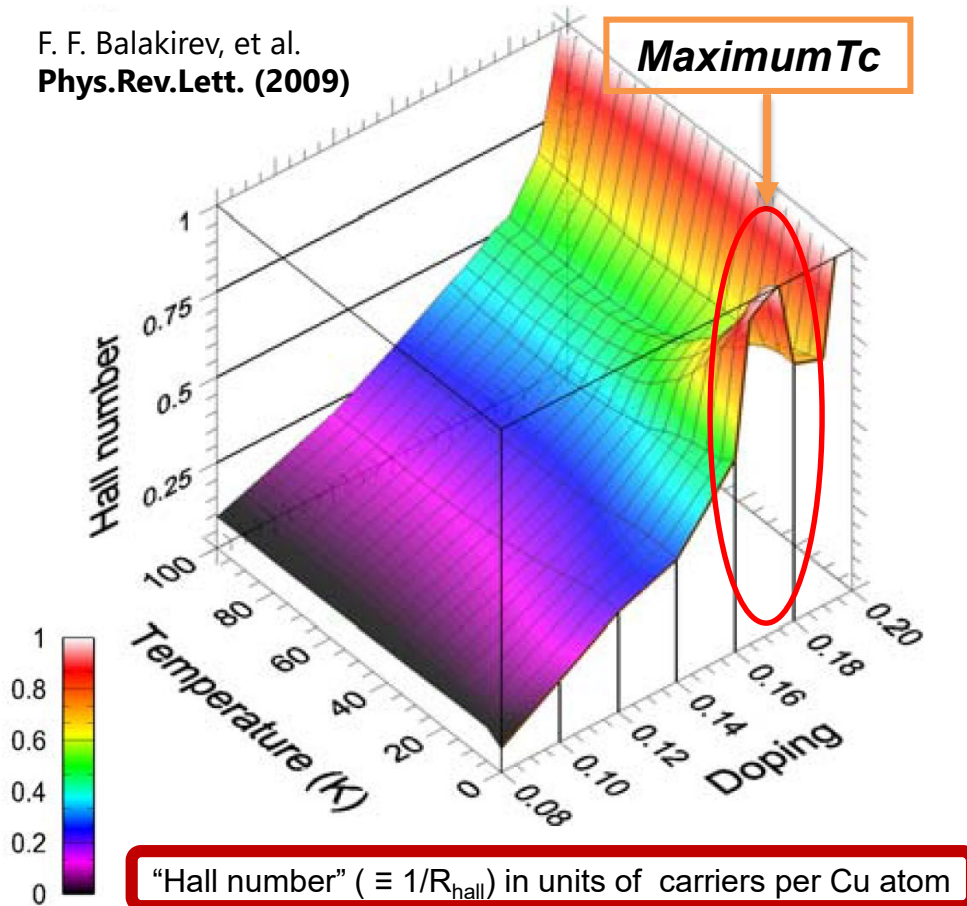
The data suggest that pockets at the center of the Brillouin zone, have stronger mass enhancement and therefore couple stronger to quantum fluctuations in the Ba122 high-temperature superconductor.

# Conclusions from High-Magnetic-Field Research

After suppressing the HTS phase, what has been discovered near optimum doping?

- Transport in LSCO and Bi-2201 finds evidence of a phase transition (peak in the Hall number)
- Transport in YBCO finds evidence of a quasiparticle mass divergence  
(quantum oscillations by Ramshaw, et al.)
- Specific heat in Ba122 finds evidence of a quasiparticle mass divergence  
(density of states recovered upon HTS suppression)

F. F. Balakirev, et al.  
**Phys.Rev.Lett. (2009)**



C.M. Moir, et al. **Nature Quantum Mat'ls (2019)**

